
Algorithm 1 Backtrack a single alignment in a recursive way

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1:  $S_1$ : Array( $m$ ),  $S_2$ : Array( $n$ ),  $M$ : Array( $m + 1$ ,  $n + 1$ ),
2: function BACKTRACKRECURSE( $i$ ,  $j$ )
3:   if  $i > 0$  and  $j > 0$  then
4:      $substitute = M[i - 1][j - 1]$ 
5:      $delete = M[i - 1][j]$ 
6:      $insert = M[i][j - 1]$ 
7:      $min = \min\{substitute, delete, insert\}$ 
8:     if  $substitute = min$  then
9:        $z = \text{BACKTRACKRECURSE}(S_1, S_2, M, i - 1, j - 1)$ 
10:       $z = \begin{pmatrix} S_1[i - 1] \\ S_2[j - 1] \end{pmatrix} \circ z$ 
11:     else if  $delete = min$  then
12:        $z = \text{BACKTRACKRECURSE}(S_1, S_2, M, i - 1, j)$ 
13:       $z = \begin{pmatrix} S_1[i - 1] \\ \varepsilon \end{pmatrix} \circ z$ 
14:     else
15:        $z = \text{BACKTRACKRECURSE}(S_1, S_2, M, i, j - 1)$ 
16:       $z = \begin{pmatrix} \varepsilon \\ S_2[j - 1] \end{pmatrix} \circ z$ 
17:     end if
18:     else if  $i > 0$  then
19:        $z = \text{BACKTRACKRECURSE}(S_1, S_2, M, i - 1, j)$ 
20:       $z = \begin{pmatrix} S_1[i - 1] \\ \varepsilon \end{pmatrix} \circ z$ 
21:     else if  $j > 0$  then
22:        $z = \text{BACKTRACKRECURSE}(S_1, S_2, M, i, j - 1)$ 
23:       $z = \begin{pmatrix} S_1[i - 1] \\ \varepsilon \end{pmatrix} \circ z$ 
24:     else
25:       return []
26:     end if
27:     return  $z$ 
28: end function
29: function BACKTRACK( $S_1$ : Array( $m$ ),  $S_2$ : Array( $n$ ),  $M$ : Array( $m + 1$ ,  $n + 1$ ))
30:   return BACKTRACKRECURSE( $S_1, S_2, M, m, n$ )
31: end function
```

Algorithm 2 Backtrack all the optimum alignments in a recursive way

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1: procedure RECURSE( $S_1$ : Array( $m$ ),  $S_2$ : Array( $n$ ),  $M$ : Array( $m + 1$ ,  $n + 1$ ),  $i$ ,  $j$ )
2:   if  $i > 0$  and  $j > 0$  then
3:      $substitute = M[i - 1][j - 1]$ 
4:      $delete = M[i - 1][j]$ 
5:      $insert = M[i][j - 1]$ 
6:      $min = \min\{substitute, delete, insert\}$ 
7:     if  $substitute = min$  then
8:        $value = \begin{pmatrix} S_1[i - 1] \\ S_2[j - 1] \end{pmatrix}$ 
9:        $z' = value \circ z$ 
10:      BACKTRACKRECURSE( $S_1$ ,  $S_2$ ,  $M$ ,  $i - 1$ ,  $j - 1$ ,  $z'$ )
11:     end if
12:     if  $delete = min$  then
13:        $value = \begin{pmatrix} S_1[i - 1] \\ \varepsilon \end{pmatrix}$ 
14:        $z' = value \circ z$ 
15:       BACKTRACKRECURSE( $S_1$ ,  $S_2$ ,  $M$ ,  $i - 1$ ,  $j$ ,  $z'$ )
16:     end if
17:     if  $insert = min$  then
18:        $value = \begin{pmatrix} \varepsilon \\ S_2[j - 1] \end{pmatrix}$ 
19:        $z' = value \circ z$ 
20:       BACKTRACKRECURSE( $S_1$ ,  $S_2$ ,  $M$ ,  $i$ ,  $j - 1$ ,  $z'$ )
21:     end if
22:     else if  $i > 0$  then
23:        $value = \begin{pmatrix} S_1[i - 1] \\ \varepsilon \end{pmatrix}$ 
24:        $z' = value \circ z$ 
25:       BACKTRACKRECURSE( $S_1$ ,  $S_2$ ,  $M$ ,  $i - 1$ ,  $j$ ,  $z'$ )
26:     else if  $j > 0$  then
27:        $value = \begin{pmatrix} \varepsilon \\ S_2[j - 1] \end{pmatrix}$ 
28:        $z' = value \circ z$ 
29:       BACKTRACKRECURSE( $S_1$ ,  $S_2$ ,  $M$ ,  $i$ ,  $j - 1$ ,  $z'$ )
30:     end if
31:     PRINT( $z$ )
32:   end procedure
33: procedure BACKTRACK( $S_1$ : Array( $m$ ),  $S_2$ : Array( $n$ ),  $M$ : Array( $m + 1$ ,  $n + 1$ ))
34:   return BACKTRACKRECURSE( $S_1$ ,  $S_2$ ,  $M$ ,  $m$ ,  $n$ , [])
35: end procedure
```
